



Investigation on the non-Darcy term in flow equations

Martin Kovács, Patrik Veleczki

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Agenda

- Darcy's equation
- Modification of Darcy's law
- Steps of the research
- Grouping & classing
- Sensitivity tests for oil and gas
- Behaviour of the β factor under changing PVT properties
- Summary table and how to use it

Darcy's equation

$$q_o = \frac{(P_e - P_{wf}) \times (k_o \times h)}{141.2 \times \mu_o B_o \left[\ln \left(0.472 \left\{ \frac{r_e}{r_w} \right\} \right) \right]}$$

$$q_g = \frac{(P_e^2 - P_{wf}^2) \times (k_g \times h)}{1.424 \times 10^3 \mu_g T z \left[\ln \left(0.472 \left\{ \frac{r_e}{r_w} \right\} \right) \right]}$$



Equation for normal fluid flow through porous medium

Neglected forces in case of low fluid velocities

Capillary force

Inertial forces

Turbulent friction force

Significant forces in case of high fluid velocities

Compression force

Gravitational force

Capillary force

Inertial forces

Turbulent friction force

Modification of Darcy's law

The equation of Forseheimer (1901)

$$-\frac{dP}{dL} = \mu \frac{v}{k} + av^2$$

The equation of Jones (1967)

For oil wells

For gas wells

$$P_e - P_{wf} = Aq_o^2 + Bq_o$$

$$A = \frac{2.30 \times 10^{-14} \times \beta B_o^2 \rho}{h^2 r_w}$$

$$B = \frac{141.2 \times \mu_o B_o \left[\ln \left(0.472 \left\{ \frac{r_e}{r_w} \right\} \right) \right]}{k_o h}$$

$$P_e^2 - P_{wf}^2 = Aq_g^2 + Bq_g$$

$$A = \frac{3.16 \times 10^{-12} \times \beta \gamma_g Tz}{h^2 r_w}$$

$$B = \frac{1.424 \times 10^3 \mu_g Tz \left[\ln \left(0.472 \left\{ \frac{r_e}{r_w} \right\} \right) \right]}{k_g h}$$

β factor:
dominant role in
the flow of the
fluids

The β factor

- inherited from the equation of Forchheimer
- causes the differences from the Darcy equation
- literature \longrightarrow lot of formula for the beta factor

Examples for the investigated β factors

Authors

Geertsma
(1974)

Pascal
(1980)

Cole & Hartman
(1998)

Equations

$$\left(\frac{0.005}{\Phi^{5.5} k^{0.5}} \right)$$

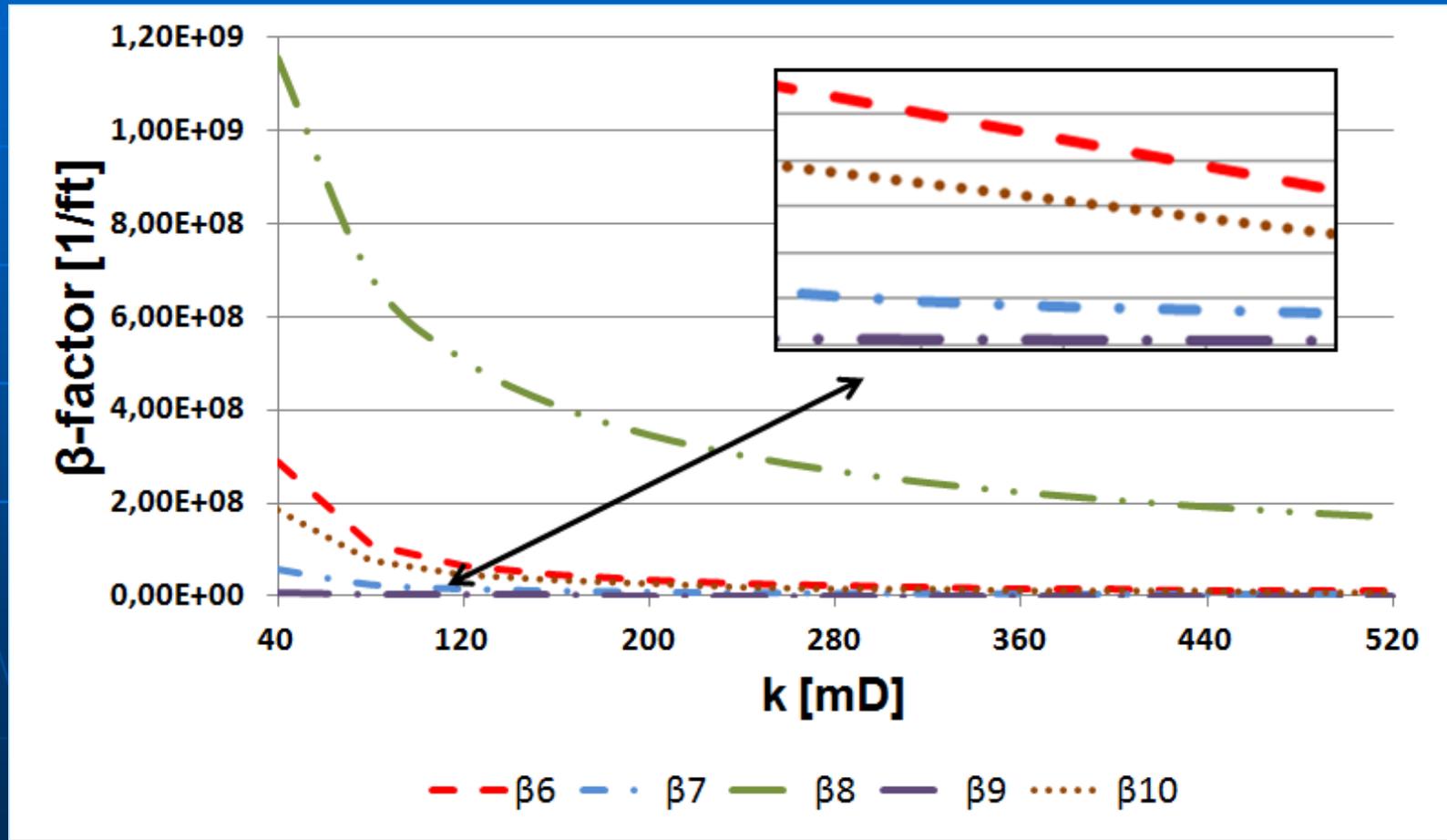
$$\left(\frac{4.8 \times 10^{12}}{k^{1.176}} \right)$$

$$\frac{8.17 \times 10^9 \Phi^{0.537}}{k^{1.79}}$$

The steps of our investigation

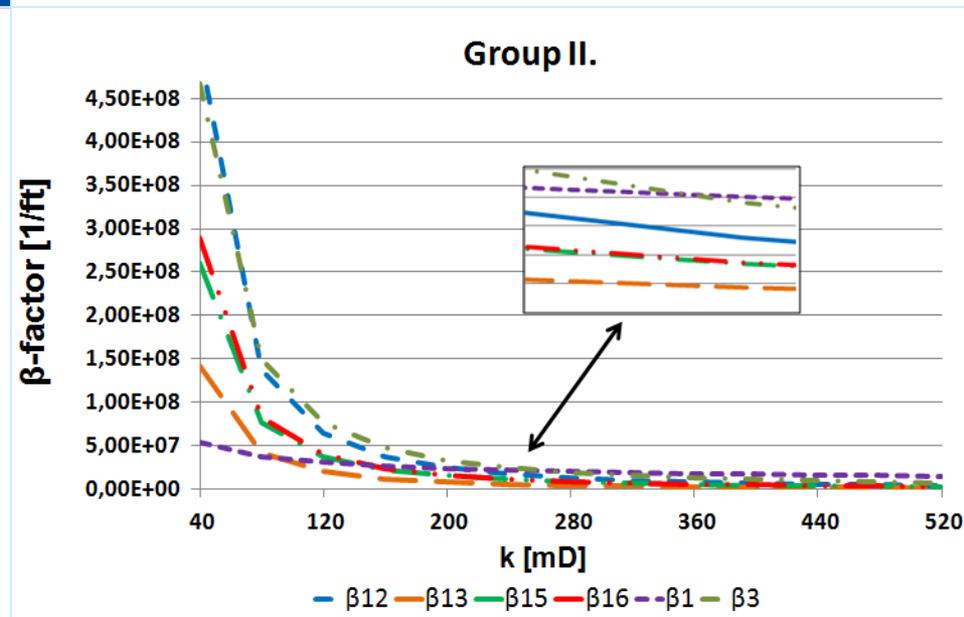
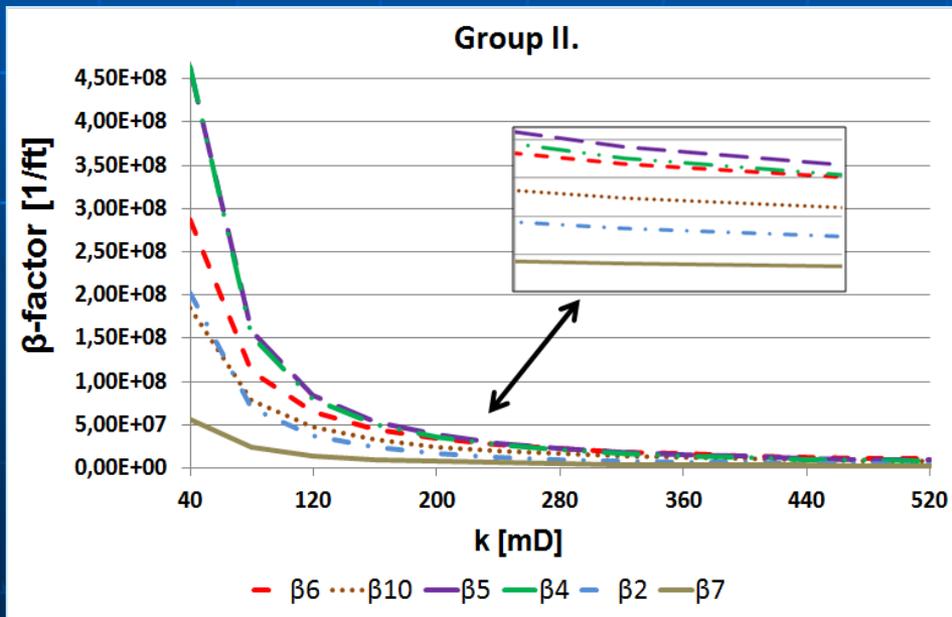
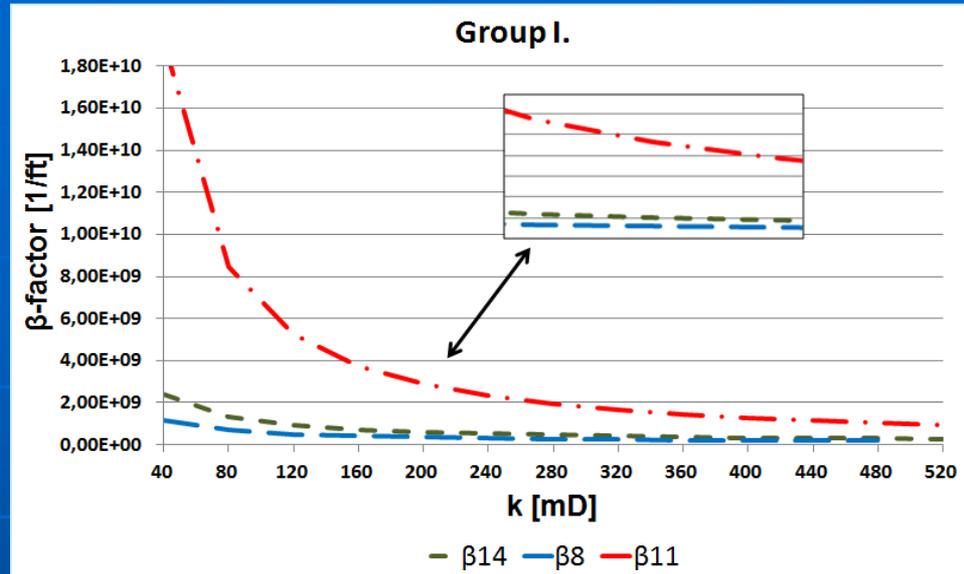
- I. Grouping & classing based on similar trends of the curves
- II. Sensitivity analysis for oil and gas wells – individual properties
- III. Sensitivity analysis for oil and gas wells – based on depth

Significant differences between the 20 β equations



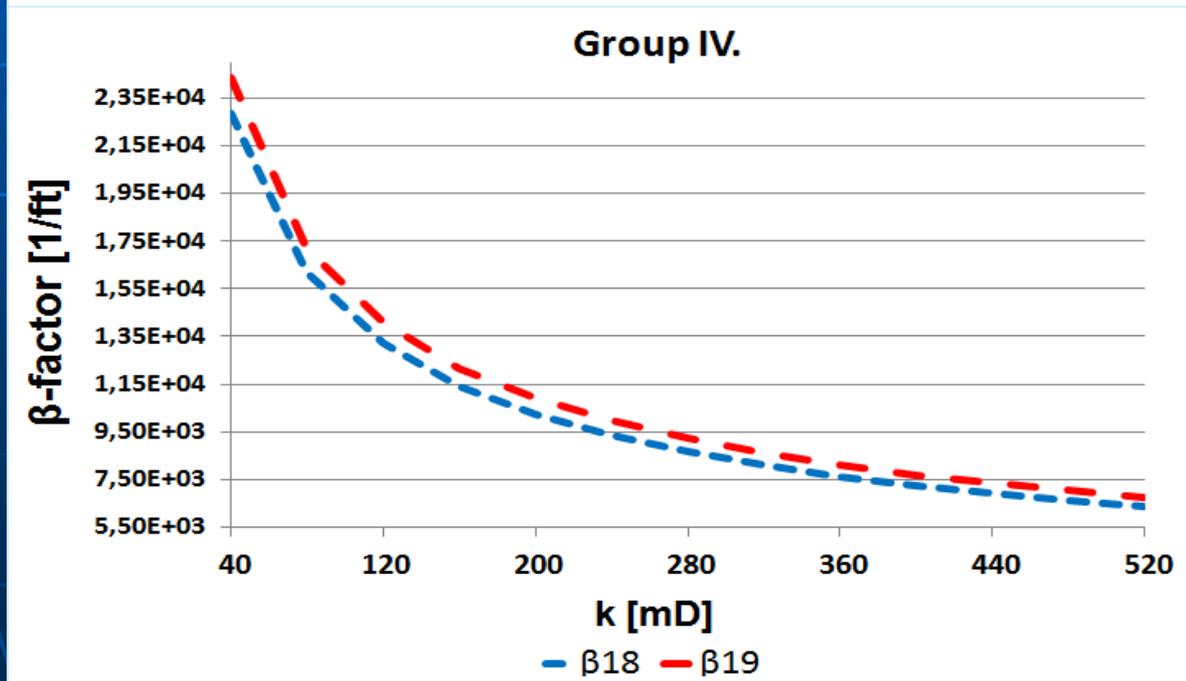
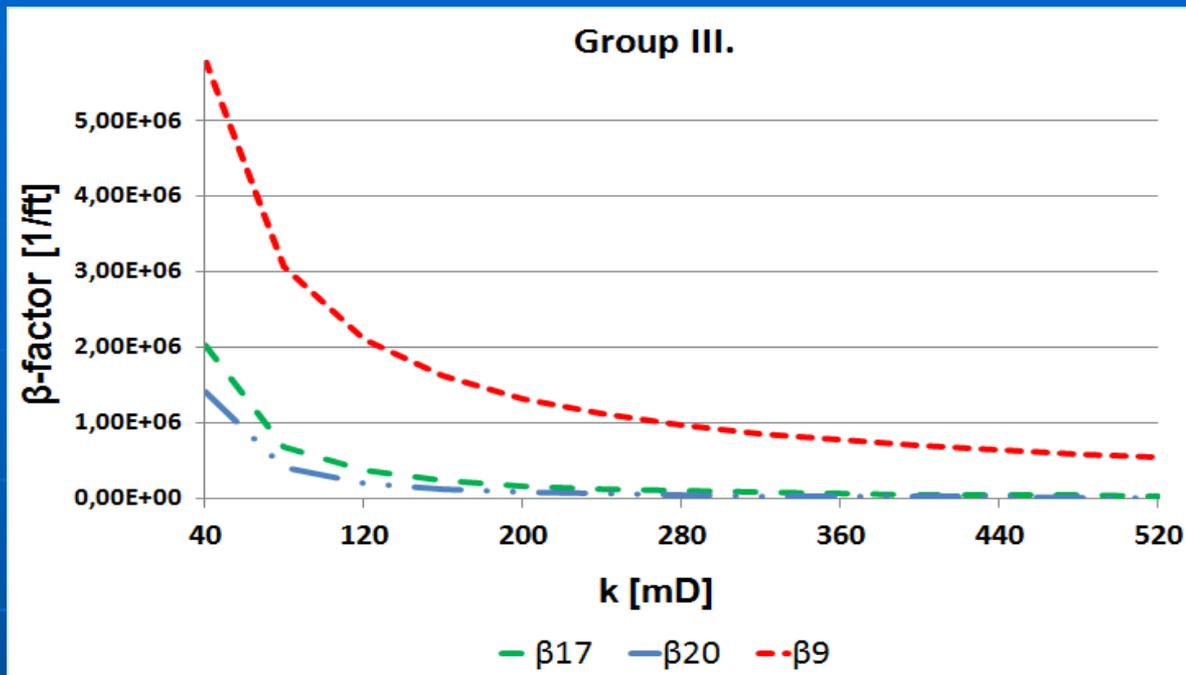
4 Groups

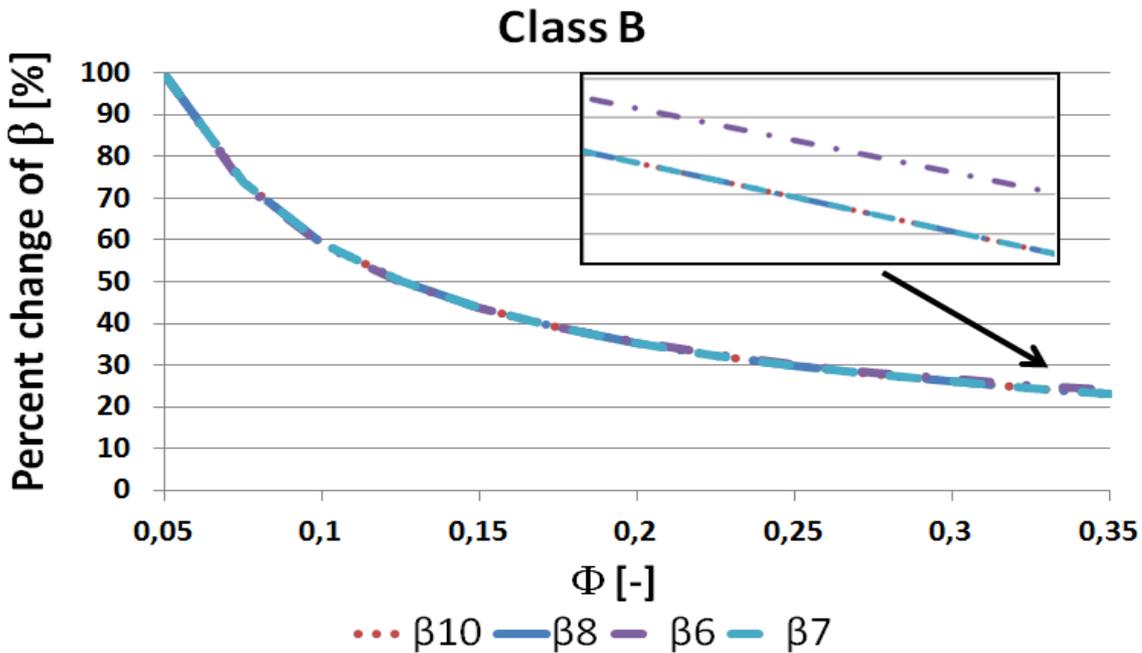
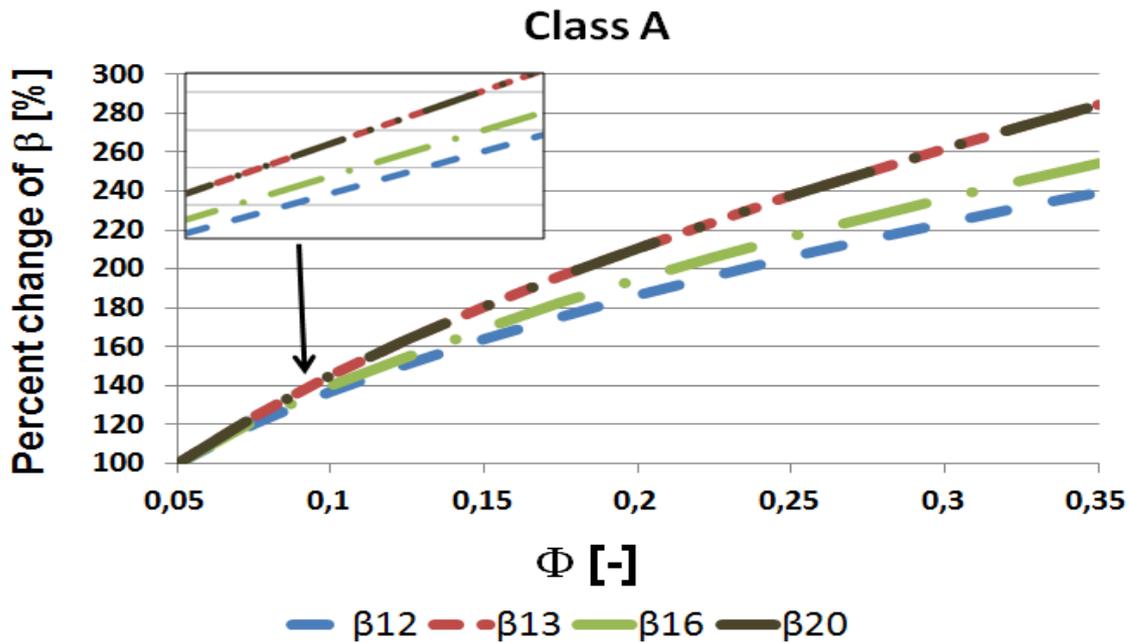
- Group I.
- Group II.



4 Groups

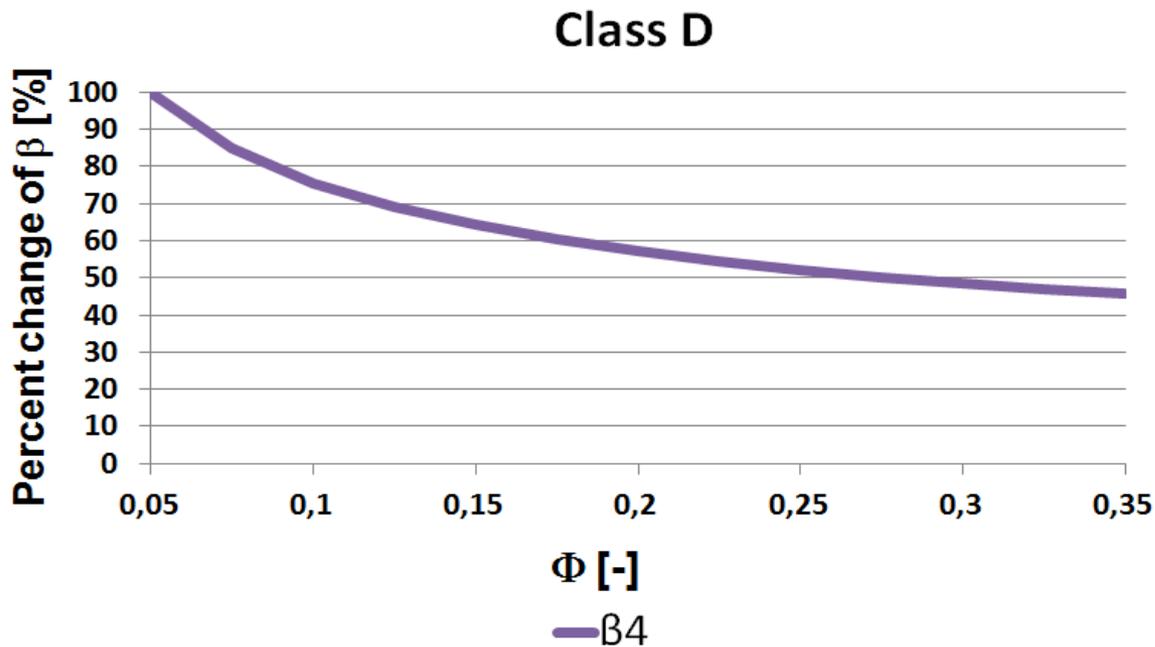
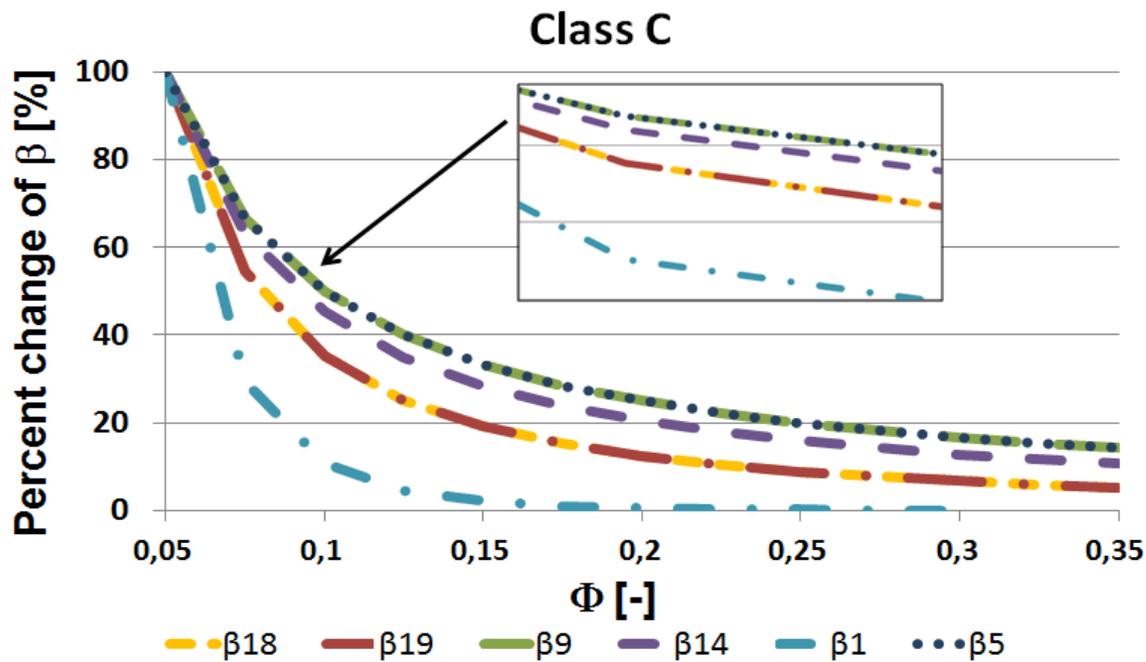
- Group III.
- Group IV.





5 Classes

- Class A
- Class B



5 Classes

- Class C
- Class D

+ Class E

Sensitivity analyzes

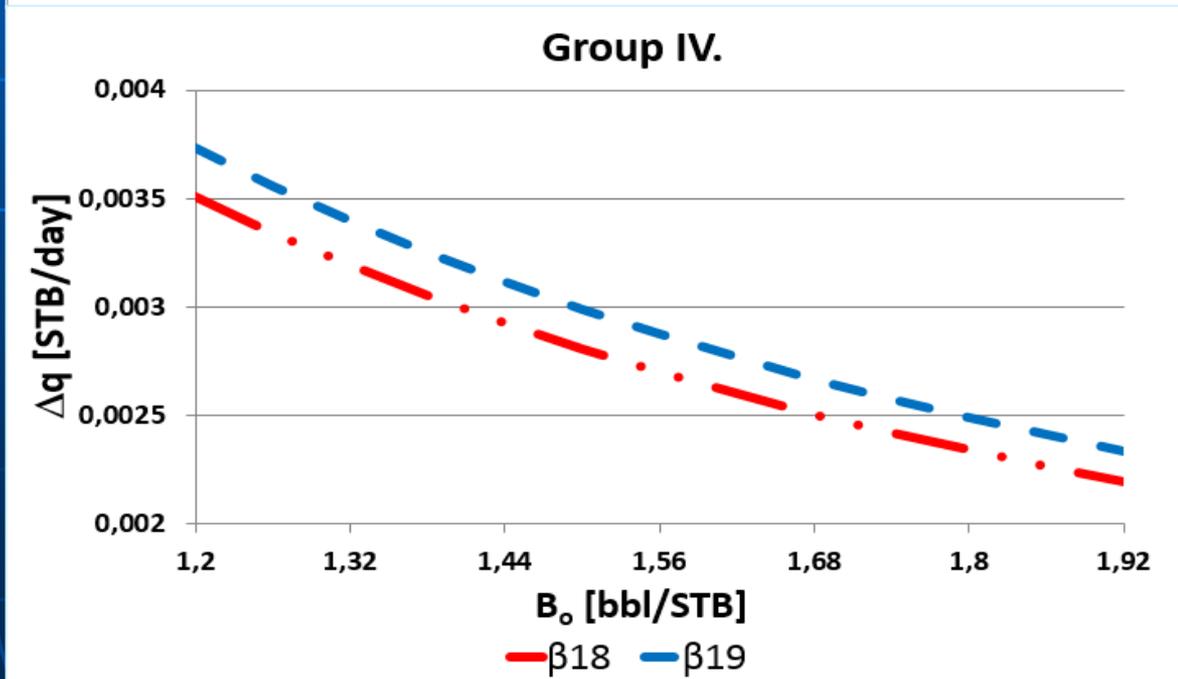
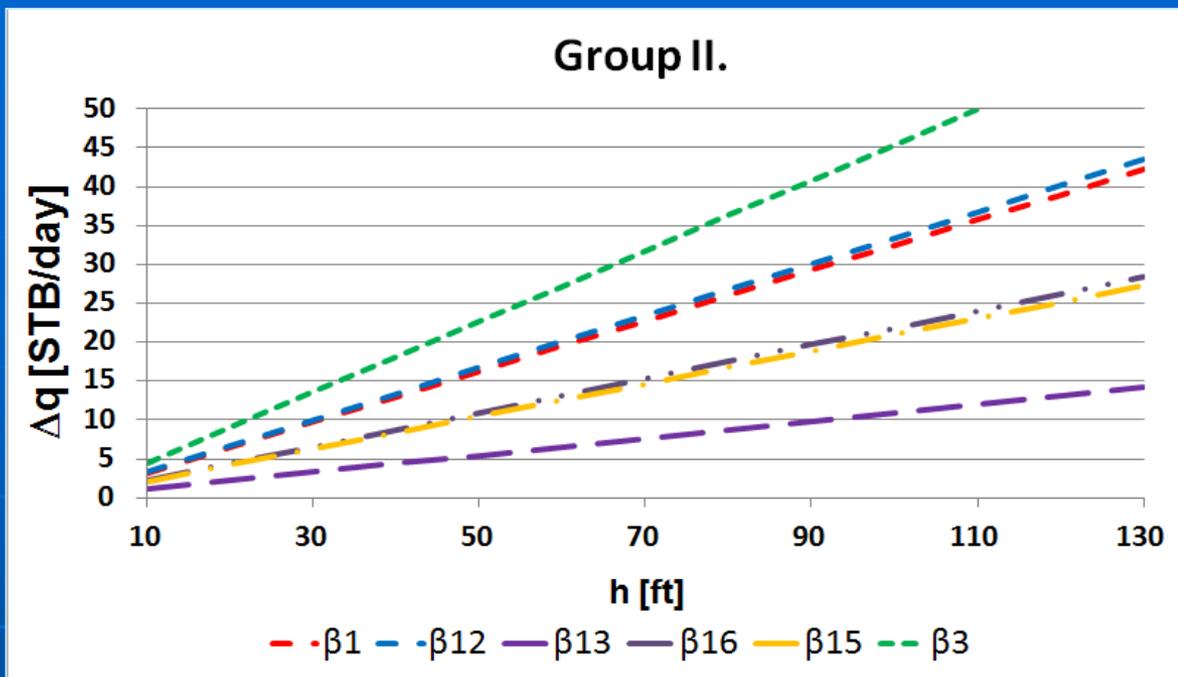
In case of oil:

- Permeability(k)
- Viscosity(μ)
- Formation volume factor(B_o)
- Reservoir thickness(h)

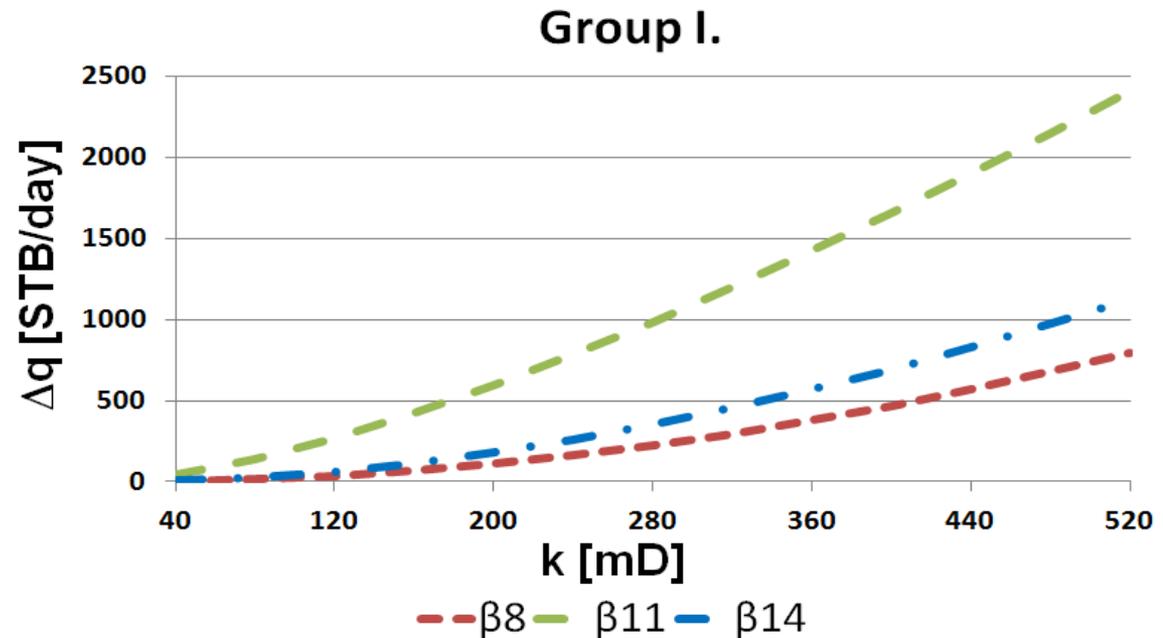
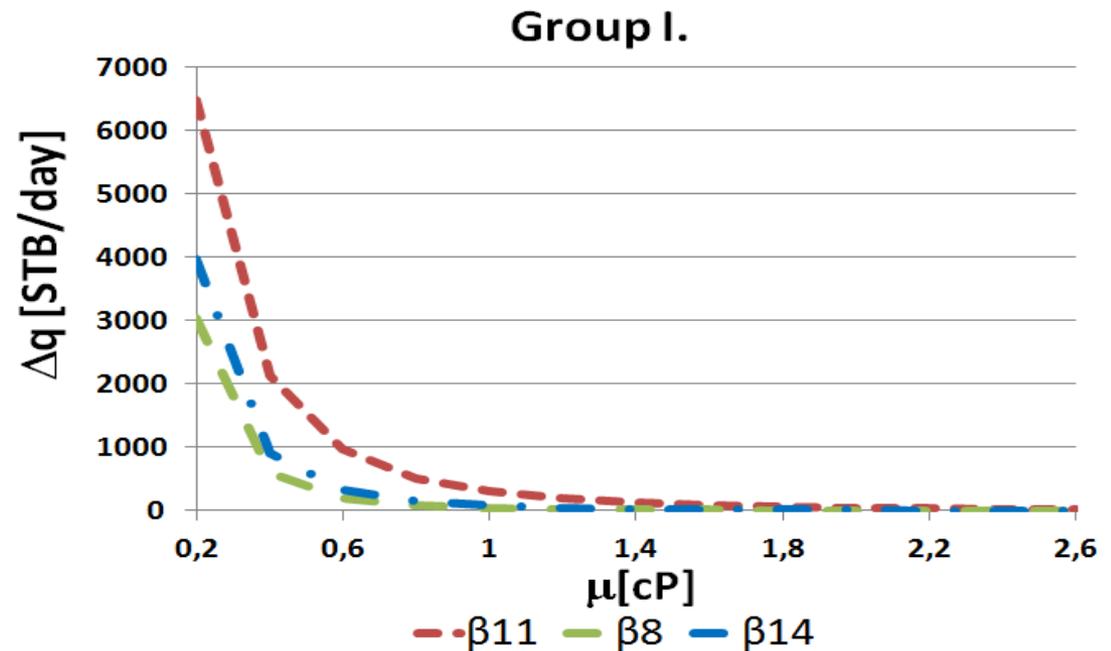
In case of gas:

- Permeability(k)
- Viscosity(μ)

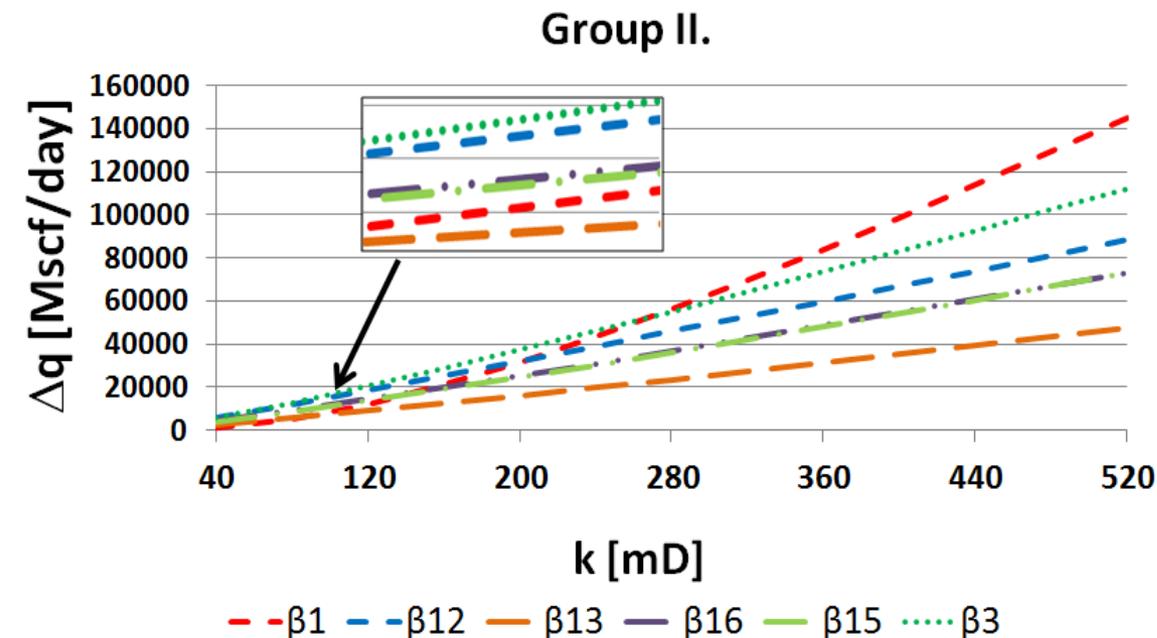
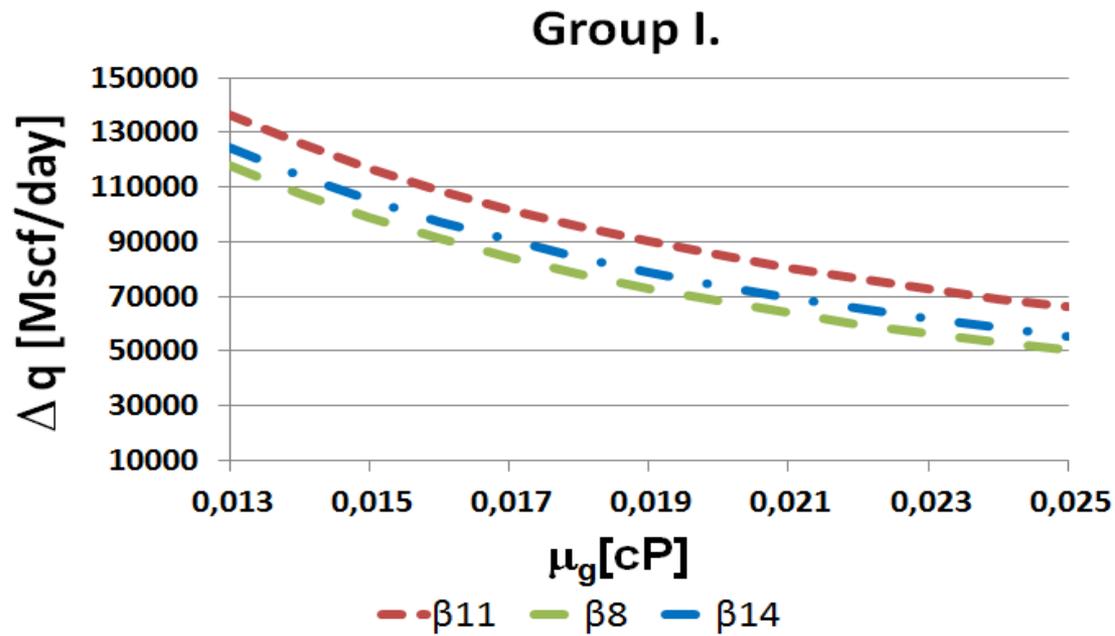
Sensitivity analyzes for OIL



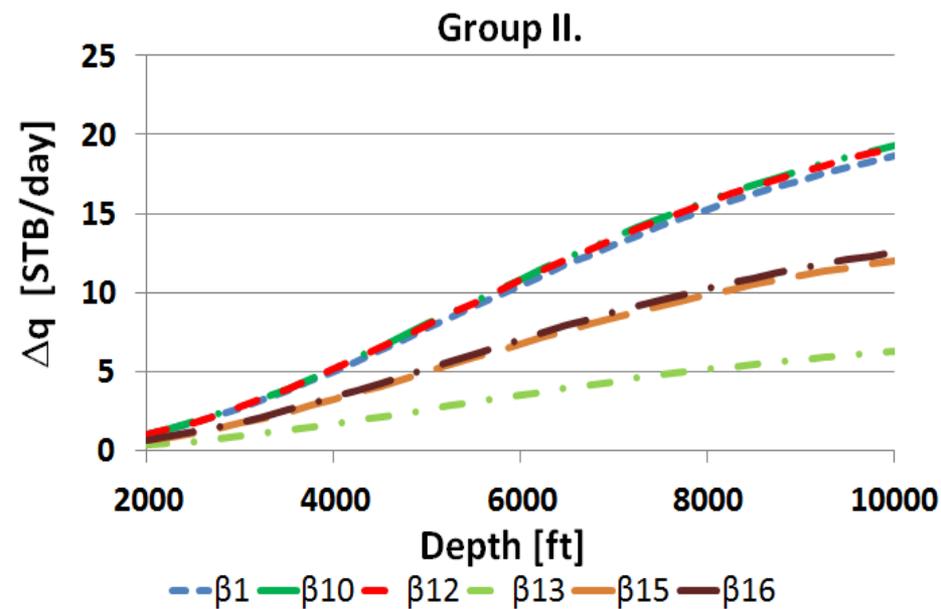
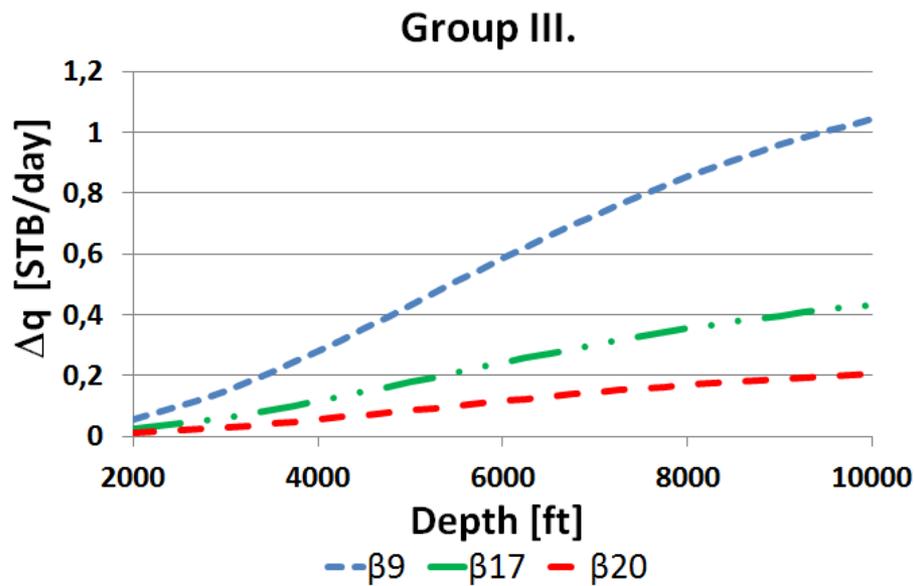
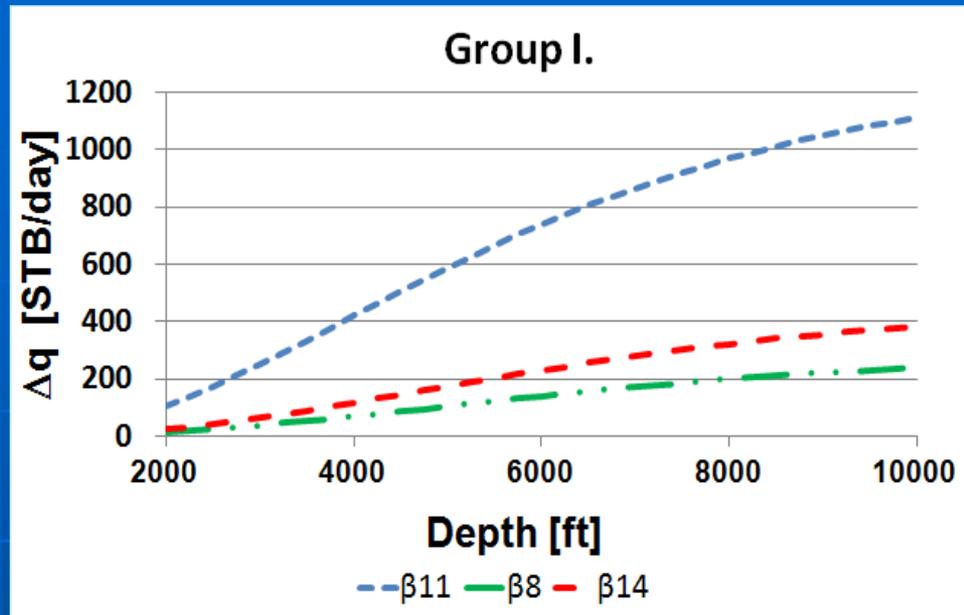
Sensitivity analyzes for OIL



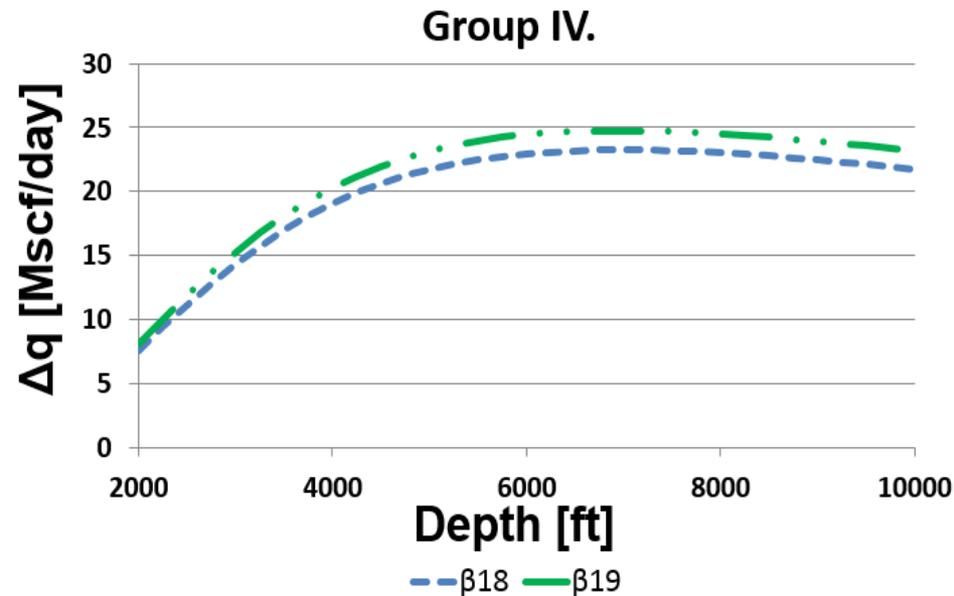
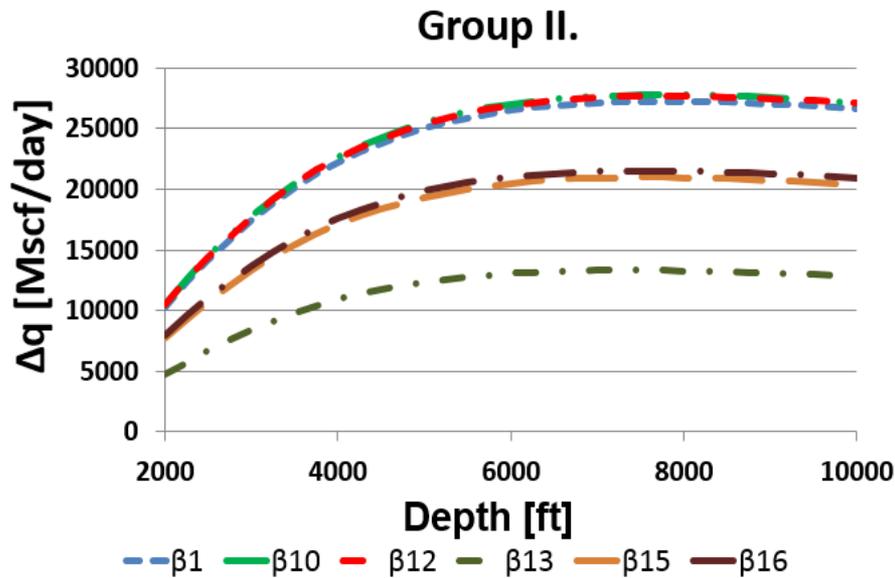
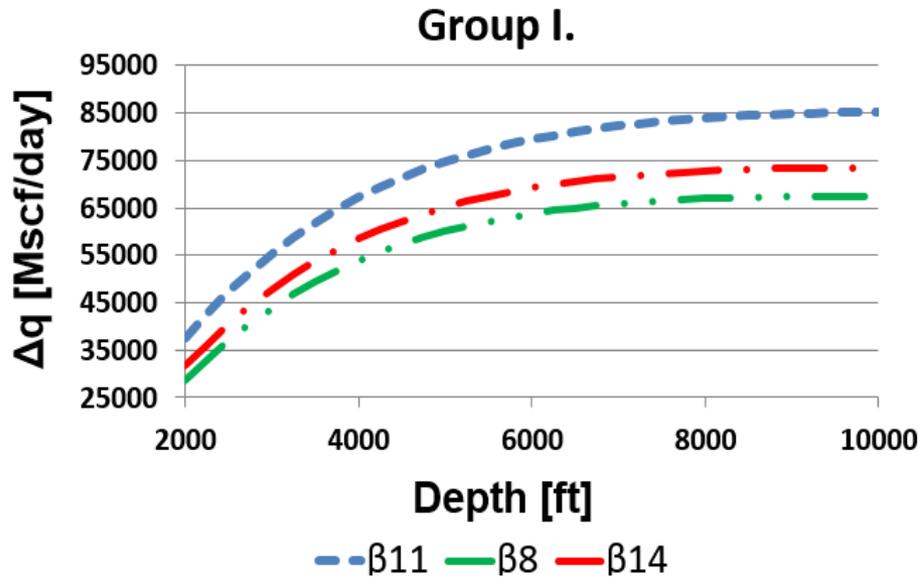
Sensitivity analyzes for GAS



Sensitivity analyzes based on the depth for OIL



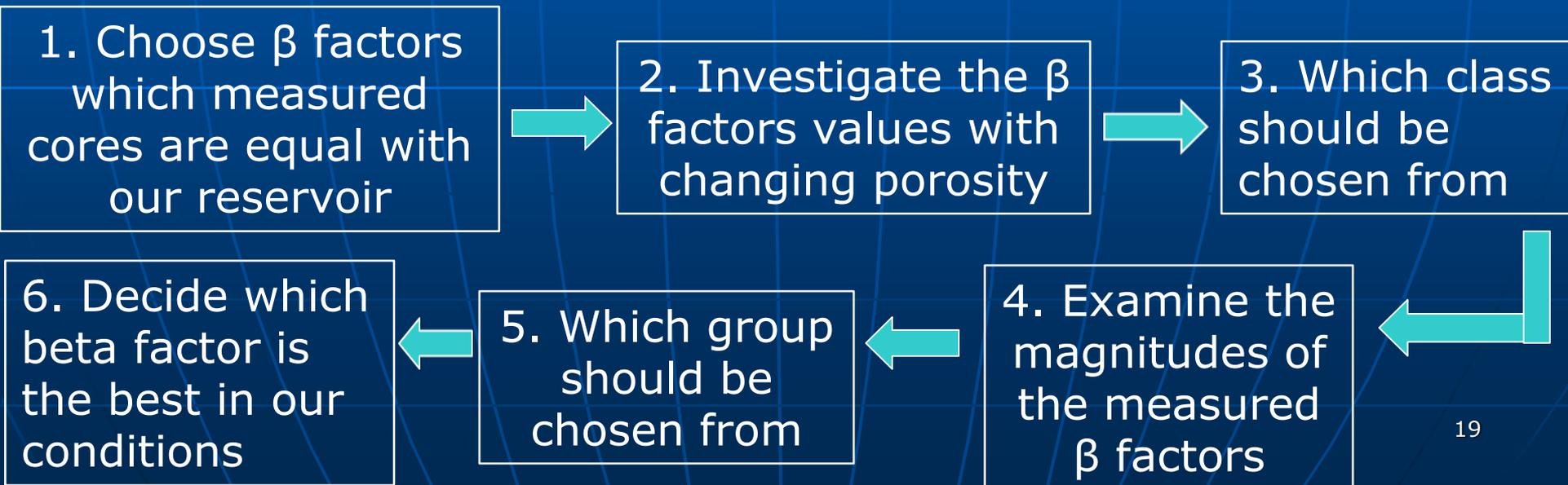
Sensitivity analyzes based on the depth for GAS



| β factor | Formula | Measurement | Group | Class |
|----------------|--|--|-------|-------|
| β_1 | $\beta_1 = \left(\frac{0.005}{\phi^{2.3} k^{0.2} \times 10^{-11}} \right) \times 30.5$ | sandstone | II. | C |
| β_2 | $\beta_2 = 6.15 \times 10^{10} (k)^{-1.22}$ | sandstone limestone | II. | E |
| β_3 | $\beta_3 = 1.98 \times 10^{11} (k)^{-1.04}$ | sandstone limestone | II. | E |
| β_4 | $\beta_4 = 7.89 \times 10^{10} (k)^{-1.02} [\phi(1 - S_w)]^{-0.404}$ | sandstone limestone | II. | D |
| β_5 | $\beta_5 = 2.11 \times 10^{10} (k)^{-1.22} [\phi(1 - S_w)]^{-1.0}$ | sandstone limestone | II. | C |
| β_6 | $\beta_6 = \frac{1}{[\phi(1 - S_w)]^2} \times e^{42 - \sqrt{(42 - 21 - 1)(\phi/(21 - 21))}}$ | sandstone limestone | II. | B |
| β_7 | $\beta_7 = \frac{5.5 \times 10^9}{k^{1.22} \phi^{0.72}} \times 0.305$ | sandstone limestone | II. | B |
| β_8 | $\beta_8 = \frac{5.5 \times 10^9}{k^{2/4} \phi^{3/4}}$ | Wilcox-homok | I. | B |
| β_9 | $\beta_9 = \left(\frac{5.123 \times 10^{-2}}{\phi} \left[\frac{1}{(1 - S_w) \sqrt{k} \times 10^{-11}} \right]^{1.227} \right) \times 30.5$ | sandstone | III. | C |
| β_{10} | $\beta_{10} = (1.82 \times 10^8 k^{-2/4} \phi^{-2/4}) \times 30.5$ | sandstone limestone dolomite | II. | B |
| β_{11} | $\beta_{11} = \left(\frac{4.8 \times 10^{11}}{k^{1.170}} \right) \times 0.305$ | Low permeability hydraulically fractured well's data | I. | E |
| β_{12} | $\beta_{12} = \frac{1.07 \times 10^{12} \times \phi^{0.449}}{k^{1.22}}$ | sandstone limestone | II. | A |
| β_{13} | $\beta_{13} = \frac{2.49 \times 10^{11} \phi^{0.227}}{k^{1.79}}$ | sandstone limestone | II. | A |
| β_{14} | $\beta_{14} = \frac{9 \times 10^9}{k^{0.7} \times \phi^{0.7}}$ | sandstone | I. | C |
| β_{15} | $\beta_{15} = \frac{17.2 \times 10^{10}}{k^{1.70}}$ | sandstone | II. | E |
| β_{16} | $\beta_{16} = \frac{4.8 \times 10^{11}}{k^{1.2} \times \phi^{-0.12}}$ | sandstone | II. | A |
| β_{17} | $\beta_{17} = \frac{2.018 \times 10^9}{k^{1.22}} \times 0.305$ | limestone, crystal limestone, well-classed sandstone | III. | E |
| β_{18} | $\beta_{18} = \frac{1}{\phi} \sqrt{\frac{1.8 \times 10^9}{k \phi}} \times 0.305$ | sandstone | IV. | C |
| β_{19} | $\beta_{19} = \frac{1}{\phi} \sqrt{\frac{245 \times 10^8}{12k \phi}} \times 0.305$ | sandstone | IV. | C |
| β_{20} | $\beta_{20} = \frac{8.17 \times 10^9 \phi^{0.227}}{k^{1.79}} \times 0.305$ | sandstone limestone | III. | A |

Results of the research

| β factor | Formula | Measurement | Group | Class |
|----------------|---|------------------------|-------|-------|
| β_1 | $\beta_1 = \left(\frac{0.005}{\phi^{5.5} k^{0.5} \times 10^{-11}} \right) \times 30.5$ | sandstone | II. | C |
| β_2 | $\beta_2 = 6.15 \times 10^{10} (k)^{-1.55}$ | sandstone limestone | II. | E |
| β_3 | $\beta_3 = 1.98 \times 10^{11} (k)^{-1.64}$ | sandstone limestone | II. | E |



References:

1. A. B. H., R. A. K., M. N. A., D. B. S. és R. I. M., „Numerical and Experimental Modeling of Non-Darcy Flow in Porous Media,” SPE, Trinidad, West Indies, 2003.
2. L. G. Jones, E. M. Blount és O. H. Glaze, „Use of Short- Term Multiple.Rate Flow Test to Predict Performance of Wells Having Turbulence, SPE6133,” SPE Annual Conference and Exhibition, New Orleans, 1967.
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4. H. Pascal, R. G. Quillian és J. Kingston, „Analisis of Vertical Fracture Length and Non-Darcy Flow Coefficient Using Variable Rate Tests,” SPE, Dallas, 1980.
5. M. F. Coles és K. J. Hartman, „Non-Darcy Measurements in Dry Core and the Effect of Immobile Liquid,” SPE Gas Technology Symposium, Calgary, Canada, 1998.

Thanks for your attention!

